

CAMBRIDGE
INTERNATIONAL EXAMINATIONS

June 2003

GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 75

SYLLABUS/COMPONENT: 9709/01

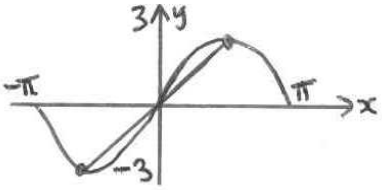
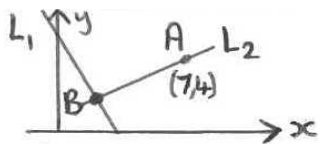
MATHEMATICS
Paper 1 (Pure 1)



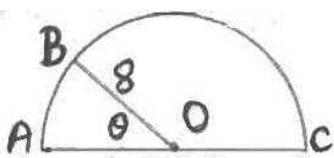
Page 1	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – JUNE 2003	9709	1

<p>1. $(2x - 1/x)^5$. 4th term needed. $\rightarrow {}_5C_3 = 5.4/2$ $\rightarrow x 2^2 x (-1)^3$ $\rightarrow -40$</p>	<p>M1 DM1 A1 [3]</p>	<p>Must be 4th term – needs $(2x)^2 (1/x)^3$ Includes and converts ${}_5C_2$ or ${}_5C_3$ Co Whole series given and correct term not quoted, allow 2/3</p>
<p>2. $\sin 3x + 2\cos 3x = 0$ $\tan 3x = -2$ $x = 38.9 (8)$ and $x = 98.9 (8)$ and $x = 158.9 (8)$</p> <p>NB. $\sin^2 3x + \cos^2 3x = 0$ etc. M0 But $\sin^2 3x = (-2\cos 3x)^2$ plus use of $s^2 + c^2 = 1$ is OK Alt. $\sqrt{5}\sin(3x + \alpha)$ or $\sqrt{5}\cos(3x - \alpha)$ both OK</p>	<p>M1 A1 A1√ A1√ [4]</p>	<p>Use of $\tan = \sin \div \cos$ with $3x$ Co For 60 + “his” For 120 + “his” and no others in range (ignore excess ans. outside range) Loses last A mark if excess answers in the range</p>
<p>3. (a) $dy/dx = 4 - 12x^{-3}$</p> <p>(b) $\int = 2x^2 - 6x^{-1} + c$</p> <p>(a) (quotient OK M1 correct formula, A1 co)</p>	<p>B2, 1 [2]</p> <p>3 x B1 [3]</p>	<p>One off for each error (4, -, 12, -3)</p> <p>One for each term – only give +c if obvious attempt at integration</p>
<p>4. $a = -10$ $a + 14d = 11$ $d = \frac{3}{2}$</p> <p>$a + (n - 1)d = 41$ $n = 35$</p> <p>Either $S_n = n/2(2a + (n - 1)d)$ or $n/2(a + l)$ $= 542.5$</p>	<p>M1 M1 A1</p> <p>M1 A1 [5]</p>	<p>Using $a = (n - 1)d$ Correct method – not for $a + nd$ Co Either of these used correctly For his d and any n</p>
<p>5. (i) $2a + b = 1$ and $5a + b = 7$ $\rightarrow a = 2$ and $b = -3$</p> <p>(ii) $f(x) = 2x - 3$ $ff(x) = 2(2x - 3) - 3$ $\rightarrow 4x - 9$ $= 0$ when $x = 2.25$</p>	<p>M1 A1 [2]</p> <p>M1 DM1 A1 [3]</p>	<p>Realising how one of these is formed Co Replacing “x” by “his $ax + b$” and “+b” For his a and b and solved $= 0$ Co</p>

Page 2	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – JUNE 2003	9709	1

<p>6. (i)</p>  <p>(ii) $x = \pi/2, y = 3$ (allow if 90°) $\rightarrow k = 6/\pi$ co.</p> <p>(iii) $(-\pi/2, -3)$ – must be radians</p>	<p>B2, 1 [2]</p> <p>M1 A1 [2]</p> <p>B1 [1]</p>	<p>For complete cycle, shape including curves, not lines, -3 to +3 shown or implied, for $-\pi$ to π. Degrees ok</p> <p>Realising maximum is $(\pi/2, 3)$ + sub Co (even if no graph)</p> <p>Co (could come from incorrect graph)</p>
<p>7. (i)</p>  <p>Gradient of $L_1 = -2$ Gradient of $L_2 = \frac{1}{2}$ Eqn of L_2 $y - 4 = \frac{1}{2}(x - 7)$</p> <p>(ii) Sim Eqns $\rightarrow x = 3, y = 2$</p> <p>$AB = \sqrt{(2^2 + 4^2)} = \sqrt{20}$ or 4.47</p>	<p>B1 M1 M1A1 [4]</p> <p>M1 A1</p> <p>M1A1 [4]</p>	<p>Co – anywhere</p> <p>Use of $m_1 m_2 = -1$</p> <p>Use of line eqn – or $y = mx + c$. Line must be through $(7, 4)$ and non-parallel</p> <p>Solution of 2 linear eqns Co</p> <p>Correct use of distance formula. Co</p>
<p>8. (i) $\overrightarrow{BA} = \mathbf{a} - \mathbf{b} = \mathbf{i} + 2\mathbf{j} - 3\mathbf{k}$ $\overrightarrow{BC} = \mathbf{c} - \mathbf{b} = -2\mathbf{i} + 4\mathbf{j} + 2\mathbf{k}$ Dot product = $-2 + 8 - 6 = 0$ \rightarrow Perpendicular</p> <p>(ii) $\overrightarrow{BC} = \mathbf{c} - \mathbf{b} = -2\mathbf{i} + 4\mathbf{j} + 2\mathbf{k}$ $\overrightarrow{AD} = \mathbf{d} - \mathbf{a} = -5\mathbf{i} + 10\mathbf{j} + 5\mathbf{k}$ These are in the same ratio \ parallel</p> <p>Ratio = 2:5 (or $\sqrt{24} : \sqrt{150}$)</p>	<p>M1 M1A1 A1 [4]</p> <p>M1</p> <p>M1</p> <p>M1A1 [4]</p>	<p>Knowing how to use position vector for \overrightarrow{BA} or \overrightarrow{BC} – not for \overrightarrow{AB} or \overrightarrow{CB}</p> <p>Knowing how to use $x_1 y_1 + x_2 y_2 + x_3 y_3$. Co</p> <p>Correct deduction. Beware fortuitous (uses \overrightarrow{AB} or \overrightarrow{CB} – can get 3 out of 4)</p> <p>Knowing how to get one of these</p> <p>Both correct + conclusion. Could be dot product = 60 \rightarrow angle = 0°</p> <p>Knowing what to do. Co. Allow 5:2</p>

Page 3	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – JUNE 2003	9709	1

<p>9.</p>  <p>(i) $\theta = 1$ angle $BOC = \pi - \theta$ Area = $\frac{1}{2}r^2\theta = 68.5$ or $32(\pi - 1)$ (or $\frac{1}{2}$circle-sector)</p> <p>(ii) $8 + 8 + 8\theta = \frac{1}{2}(8 + 8 + 8(\pi - \theta))$ Solution of this eqn $\rightarrow 0.381$ or $\frac{1}{3}(\pi - 2)$</p> <p>(iii) $\theta = \pi/3$ AB = 8cm BC = $2 \times 8 \sin \pi/3 = 8\sqrt{3}$ Perimeter = $24 + 8\sqrt{3}$</p>	<p>B1 M1 A1 [3]</p> <p>M1 M1 A1 [3]</p> <p>B1 M1 A1 [3]</p>	<p>For $\pi - \theta$ or for $\frac{1}{2}\pi r^2$ – sector Use of $\frac{1}{2}r^2\theta$ Co NB. 32 gets M1 only</p> <p>Relevant use of $s = r\theta$ twice Needs θ – collected – needs perimeters Co. [3]</p> <p>Co. Valid method for BC – cos rule, Pyth allow decimals here Everything OK. Answer given NB. Decimal check loses this mark</p>
<p>10. $y = \sqrt{(5x + 4)}$</p> <p>(i) $dy/dx = \frac{1}{2}(5x + 4)^{-1/2} \times 5$ $x = 1$, $dy/dx = 5/6$</p> <p>(ii) $dy/dt = dy/dx \times dx/dt$ $= 5/6 \times 0.03$ $\rightarrow 0.025$</p> <p>(iii) realises that area \rightarrow integration $\int = (5x + 4)^{3/2} \div \frac{3}{2} \div 5$ Use of limits $\rightarrow 54/15 - 16/15$ $= 38/15 = 2.53$</p>	<p>B1B1 B1 [3]</p> <p>M1</p> <p>A1√ [2]</p> <p>M1</p> <p>A1A1</p> <p>DM1 A1 [5]</p>	<p>$\frac{1}{2}(5x + 4)^{-1/2} \times 5$ B1 for each part Co</p> <p>Chain rule correctly used</p> <p>For (i) $\times 0.03$</p> <p>Realisation + attempt – must be $(5x + 4)^k$</p> <p>For $(5x + 4)^{3/2} \div \frac{3}{2}$. For $\div 5$</p> <p>Must use “0” to “1” Co</p>

Page 4	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – JUNE 2003	9709	1

<p>11. (i) $8x - x^2 = a - x^2 - b^2 - 2bx +$ equating $\rightarrow b = -4$ $a = b^2 = 16$ (i.e. $16 - (x - 4)^2$)</p> <p>(ii) $dy/dx = 8 - 2x = 0$ when $\rightarrow (4, 16)$ (or from $-b$ and a)</p> <p>(iii) $8x - x^2 \geq -20$ $x^2 - 8x - 20 = (x - 10)(x + 2)$ End values -2 and 10 Interval $-2 \leq x \leq 10$</p> <p>$g: x \rightarrow 8x - x^2$ for $x \geq 4$</p> <p>(iv) domain of g^{-1} is $x \leq 16$ range of g^{-1} is $g^{-1} \geq 4$</p> <p>(v) $y = 8x - x^2 \rightarrow x^2 - 8x + y = 0$</p> <p>$x = 8 \pm \sqrt{(64 - 4y)} \div 2$ $g^{-1}(x) = 4 + \sqrt{(16 - x)}$</p> <p>or $(x - 4)^2 = 16 - y \rightarrow x = 4 + \sqrt{(16 - y)}$ $\rightarrow y = 16 - (x - 4)^2$</p>	<p>M1 B1 A1 [3]</p> <p>M1 A1 [2]</p> <p>M1 A1 A1 [3]</p> <p>B1✓ B1 [2]</p> <p>M1</p> <p>DM1 A1 [3]</p>	<p>Knows what to do – some equating Anywhere – may be independent For $16 - ()^2$</p> <p>Any valid complete method Needs both values</p> <p>Sets to 0 + correct method of solution Co – independent of $<$ or $>$ or $=$ Co – including \leq ($<$ gets A0)</p> <p>From answer to (i) or (ii). Accept <16 Not f.t since domain of g given</p> <p>Use of quadratic or completed square expression to make x subject</p> <p>Replaces y by x Co (inc. omission of $-$)</p>
---	--	---